

1 **Title**

2 Thermionic Transport Across Gold-Graphene-WSe₂ van der Waals Heterostructures

3

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20

21 **Abstract**

22 Solid state thermionic devices based on van der Waals structures were proposed for nanoscale
23 thermal to electrical energy conversion and integrated electronic cooling applications. We study
24 thermionic cooling across gold-graphene-WSe₂-graphene-gold structures computationally and
25 experimentally. Graphene and WSe₂ layers were stacked, followed by deposition of gold contacts.

26 The I-V curve of the structure suggests near Ohmic contact. A new technique which combines
27 thermoreflectance and cooling curve measurements is used to extract the device ZT. The measured
28 Seebeck coefficient, thermal and electrical conductance and ZT values at room temperatures are in
29 agreement with the theoretical predictions using first principles calculations combined with real
30 space Green's function formalism. Finally, we discuss the design strategies and lay the pathway
31 toward efficient thermionic devices.

32

33 **Introduction**

34 Solid-state thermionic (SSTI) power generators can be viewed as intermediate between vacuum-
35 state thermionic converters and thermoelectric power generators. Like many other heat engines,
36 these devices can work either as power generators where they convert input heat to electricity, or
37 coolers where applied electricity is used to pump heat. The SSTI power generators and refrigerators
38 were first proposed by Shakouri (1) and Mahan (2) independently as an alternative to vacuum state
39 thermionic converters. These devices are made by inserting a semiconducting layer between
40 metallic electrodes. The semiconducting layer forms an energy barrier for charge carriers allowing
41 only hot ones to pass (3-5). This current flow is referred to as thermionic current. The SSTI devices
42 are similar to vacuum state thermionic ones wherein the vacuum is replaced by the semiconducting
43 layer. Due to the lower energy barrier, the SSTI devices operate at temperatures much smaller than
44 the vacuum state thermionic devices. The SSTI devices are also very similar to thermoelectric
45 devices. The most important difference is that the thermionic transport in SSTI devices is ballistic,
46 whereas the thermoelectric transport is diffusive. Like thermoelectric devices, it is possible to
47 define an equivalent figure of merit, ZT for SSTI devices. The figure of merit concept is borrowed
48 from the thermoelectric field and is defined as $ZT = \frac{\sigma S^2 T}{\kappa}$, where σ is the electrical conductivity, S
49 is the Seebeck coefficient and κ is the thermal conductivity. We note that the energy conversion
50 efficiency and the coefficient of performance (COP) equations of SSTI devices are not the same as

the ones for thermoelectric devices (2, 6). Only after linearizing the equations (that is under small temperature drops and small voltage drops), an analogy to thermoelectric modules could be drawn. In this analogy, the Seebeck coefficient is the energy barrier height (in units of volt) divided by the temperature plus a constant. It can be shown numerically that thermoelectric equations can reproduce thermionic results accurately, which is a remarkable observation by Mahan (2). Theoretical investigations had conflicting predictions comparing the efficiency of SSTI converters to those of thermoelectric devices (1,2, 6-8). In SSTI converters, in order to maintain ballistic transport of the hot electrons, the semiconducting layer thickness, L , should be equal or less than the electron mean free path, λ . On the other hand, a minimum length, L_t , is needed to suppress the tunneling of electrons, which is undesirable since low energy electrons (with energies smaller than the chemical potential, μ) act as holes and lower the efficiency of the electron transmitting device (similar to bipolar effect in the case of thermoelectric transport). Thus, the semiconducting layer thickness should satisfy the condition: $L_t < L < \lambda$.

Recently, highly efficient SSTI converters made out of 2D layered materials were proposed theoretically and computationally (7, 9, 10). In these structures, the in-plane atoms are covalently bonded while the layers in the cross-plane direction, are weakly bonded by van der Waals forces. Due to weak interlayer bonding, it is possible to stack different 2D materials on top of each other without any strain that would otherwise develop because of lattice mismatch in the presence of a strong bonding (11). Bandgap of 2D materials can be tuned by applying strain, electric field and also by changing the number of stacked layers. Arsenene, the monolayer of arsenic, for example, have been reported to show a smooth transition from semi-metallic to semiconducting state for different number of stacked layers (12). It is also reported that, arsenene, an indirect bandgap semiconductor can be converted to a direct bandgap semiconductor by applying compressive and tensile strain along its a-axis (12). Another important property of 2D layered heterostructures is

76 their low value of thermal conductance in the cross-plane direction which is the result of the weak
 77 van der Waals interlayer bonding. In solid-state thermionic devices, the thermal conductance should
 78 be minimized and extremely small values of $0.1 \text{ MWm}^{-2}\text{K}^{-1}$ are desirable for achieving high
 79 efficiency (13). The main challenge is to achieve these small conductance values at small length
 80 scales to preserve the ballistic nature of thermionic transport. Extremely small conductance values
 81 have already been demonstrated in several 2D layered structures and at nanometer length scales.
 82 For example, Yuan *et al.* reported thermal conductance values smaller than $1 \text{ MWm}^{-2}\text{K}^{-1}$ across
 83 seven layers of MoS₂ (14). Zhang *et al.* estimated the interfacial thermal conductance across
 84 monolayer and bilayer MoSe₂ to be of the order $0.1\text{--}1 \text{ MWm}^{-2}\text{K}^{-1}$ (15). Massicotte *et al.* reported
 85 a cross-plane thermal conductance of $0.5 \text{ MWm}^{-2}\text{K}^{-1}$ across graphene-WSe₂-graphene
 86 heterostructure that were tested for photo-thermionic emission (16). Chen *et al.* reported a low
 87 thermal conductance of $2.36 \text{ MWm}^{-2}\text{K}^{-1}$ for Graphene-h-BN-graphene heterostructure (17). In
 88 this structure, h-BN forms too high of an energy barrier for electrons and results in poor electronic
 89 properties. Therefore, the structure's figure of merit at room temperature is only on the order of 10^{-6} .
 90 To our knowledge, this is the only experimentally measured ZT for layered structures across few
 91 nanometers.

92
 93 Due to lack of well-established measurement methods (18, 19), currently, there are very few
 94 experimental studies focused on the efficiency of the solid-state thermionic converters made out of
 95 2D van der Waals heterostructures. In this paper, we study thermionic transport across a gold-
 96 graphene-3 layers of WSe₂-graphene-gold (Au-Gr-3WSe₂-Gr-Au) structure computationally and
 97 experimentally. We report a new experimental technique which combines the thermorefectance
 98 and cooling curve measurements to extract the equivalent figure merit of the SSTI converter.
 99 Although our measured room temperature figure of merit is small ($ZT = 1.5 \times 10^{-3}$), this value is
 100 three orders of magnitude higher than previously reported value for similar types of 2D

101 heterostuctures (17). The experimental values are in close agreement with the theoretical values
102 calculated for this structure.

103

104 **Results**

105 Electrical Transport: Au-Gr-3WSe₂-Gr-Au device was fabricated on Si/SiO₂ substrate where the
106 device structure is illustrated on Fig. 1A. A bottom graphene layer, a 3-layers WSe₂ and a top
107 graphene layer were mechanically exfoliated and transferred on the substrate in sequence using a
108 polydimethylsiloxane (PDMS)-assisted transfer method. The thickness of WSe₂ was identified by
109 using optical contrasts on an optical microscope image of the WSe₂ on the PDMS where thicknesses
110 of reference samples (from 1 to 5 layers) were measured by atomic force microscopy (AFM) and
111 their optical contrasts in the green channel of a charge coupled device camera were served as
112 reference values. Metal electrodes (Ti/Au-3nm/100nm) were deposited by using a general
113 photolithography process and an electron-beam evaporation. The fabricated device was annealed at
114 200°C in a vacuum chamber overnight to achieve the Ohmic contact between metal and graphene.
115 The optical microscope image of the fabricated device is shown in **Error! Reference source not**
116 **found.B**, and **Error! Reference source not found.C** shows the current-voltage characteristic
117 measured across the top and bottom metal contacts, indicating a near-Ohmic contact. Our further
118 analysis show that the measured value is dominated by the contact resistance between Au/Ti and
119 graphene (see supplementary materials).

120

121 The room-temperature Seebeck coefficient of this structure is measured by the set-up schematically
122 shown in Fig. 2A. A small external heater was placed close to one of the metallic pads to create a
123 local hot spot. We then used two thermocouples and two electrical probes directly connected to the
124 gold pads (contacts) to simultaneously measure the temperature differential and the Seebeck voltage
125 across the Au-Gr-WSe₂-Gr-Au device. The device-level Seebeck coefficient can be estimated by

126 linearly fitting the measured Seebeck voltage (μV) with respect to the measured temperature
127 differential ΔT ($^{\circ}\text{K}$) as shown in Fig. 2B. It is noted that the data suffers from a large noise due to
128 non-uniformity of the induced temperature gradient across the sample. Nevertheless, our obtained
129 experimental Seebeck coefficient $\sim 72 \pm 12 \mu\text{V/K}$ is in good agreement with the theoretically
130 calculated value of $86 \mu\text{V/K}$ using first principles and Green's function calculations.

131
132 We note that measured Seebeck coefficient should be interpreted as the device-level Seebeck
133 coefficient and includes contributions from the graphene ribbons as well as the Gr-3WSe₂-Gr
134 overlap region. While it is not possible to separate the contribution of these two regions, we note
135 that the majority of the Seebeck signal is from the overlap region. The thermal resistance of the
136 overlap region is much larger than the graphene ribbons, hence the majority of the temperature drop
137 is on the overlap region.

138
139 Thermionic transport across Au-Gr-WSe₂-Gr-Au structure with 3-5 layers of WSe₂ is studied
140 computationally using first principles calculations combined with real space Green's function
141 formalism. The schematic of the studied structure is shown in Fig. 3A and the local density of states
142 of the structure is shown in **Error! Reference source not found.**B. The energy barrier height is
143 about 0.1 eV. It is expected that optimal barrier height for thermionic application is around $2k_{\text{B}}T$
144 (6), therefore it is expected that this device works best at temperatures above 600 $^{\circ}\text{K}$. To reduce the
145 energy barrier, one way is to replace gold with another metal with larger work function. Fig. 3C
146 shows the calculated local density of states for platinum with larger work function which is a better
147 match to the work function of the current structure and hence has a lower energy barrier. In addition,
148 platinum has a larger density of the states at the Fermi level resulting in higher carrier conductance.
149 The electronic transmission function of both gold and platinum structures are shown in Fig. 4A.
150 Both structures show a clear gap when more than 3 layers of WSe₂ are present indicating that three

151 layers are enough to suppress the tunneling current. Using the density of the state and the
 152 transmission function, the electronic transport properties could be calculated using linear response
 153 integrals. The results indicates a very small electrical conductance value of 3.5×10^{-5} in units of
 154 quantum conductance for Au-Gr-3WSe₂-Gr-Au structure. This value is equivalent to resistance
 155 times area of $3.7 \times 10^{-10} \Omega m^2$ which is too small for an efficient performance. The conductance is
 156 greatly enhanced when gold is replaced by platinum as shown in Fig. 4B due to lower energy barrier
 157 of platinum structure. The calculated equivalent Seebeck coefficient of Au-Gr-3WSe₂-Gr-Au
 158 structure is 86 $\mu V/K$ at room temperatures consistent with our experimentally measured value
 159 and increases to 292 $\mu V/K$ at high temperatures ($T \sim 700^\circ K$).
 160

161 Thermal transport: Due to the large size of the supercell, full first principles calculations of lattice
 162 thermal conductance values are too costly for the current structure. Therefore, we used a simpler
 163 1D model as described in our previous publication (9). The calculated phonon thermal conductance
 164 of Au-Gr-3WSe₂-Gr-Au is about 14 $MWm^{-2}K^{-1}$. Due to the ballistic nature of transport, at
 165 temperatures above 200°K, the thermal conductance values do not change significantly as shown
 166 in Fig. 4D. The electronic part of the thermal conductance is an order of magnitude smaller
 167 compared to the lattice part at room temperatures but reaches to 0.2 $MWm^{-2}K^{-1}$ at 680K. Finally,
 168 overall ZT is small. The calculated electronic and phononic transmission functions, the Seebeck
 169 coefficient, the electrical and thermal conductance are shown in Fig. 4. As mentioned, the small
 170 electronic conductance is the main drawback of the current structure. To demonstrate the
 171 importance of the metallic contact, we also report theoretical results of replacing gold with
 172 platinum. Due to improved conductance values, platinum structure shows a much larger ZT values
 173 as shown in the supplementary materials.
 174

175 To check the validity of theory, we used time domain thermoreflectance (TDTR) measurements to
176 experimentally measure the thermal conductance of the fabricated device (20). We deposit a
177 nominal 80 nm thick aluminum layer via electron-beam evaporation to serve as transducer for the
178 Gr-3WSe₂-Gr device. The measured resistance thus encompasses contributions from the Al-Gr
179 interface, the Gr-3WSe₂-Gr structure, and the Gr-SiO₂ interface. The measured conductance
180 accounting for each of these contributions is determined to be 9 MWm⁻²K⁻¹. We also measure the
181 conductance of the Al-Gr-SiO₂ interface, and determine this to be 20 MW m⁻² K⁻¹. Using a series
182 resistor model, discussed further in the Supplemental Material, the thermal conductance of Gr-
183 WSe₂-Gr layer can be extracted to be 17 MWm⁻²K⁻¹. This is in good agreement with the
184 theoretically calculated value. We note that the Au-Gr contacts are not included in the experiment
185 and if included, they will lower the overall thermal conductance value.

186
187 Finally, we evaluate the device-level ZT by directly measuring the cooling curve of the device using
188 a thermoreflectance imaging technique. We borrow the cooling curve concept from the
189 thermoelectric field. This measurement is done routinely for testing the device performance of
190 thermoelectric devices. The principle is as follows: A temperature difference develops as a result
191 of applying an electric current to a Peltier module. This temperature difference is due to the Peltier
192 effect and the Joule heating. The temperature difference is measured at steady state for a range of
193 applied currents. It is shown that the maximum cooling (ΔT_m) is achieved when the cold side is
194 fully isolated (zero heat flux), the hot side is connected to a heat sink (constant temperature
195 boundary conditions) and the current is equal to $I_{opt} = \frac{ST_C}{R}$ where T_C is the temperature on the cold
196 side, and R is the resistance of the device. Under these conditions, ΔT_m is proportional to the ZT
197 of the device following Eq. (1) (21, 22):

198

$$ZT = \frac{2\Delta T_m}{T_c} \quad (1)$$

To perform cooling curve measurements, we use thermoreflectance technique wherein a pulsed voltage is applied across the device and the 2D temperature profile of the device is obtained by mapping the local changes in the reflectance coefficient to the local temperature. To help visually perceive the thermal condition in the device under bias for thermoreflectance imaging, we demonstrate the temperature mapping of the device under a relatively large pulsed voltage of 2V, shown in Fig. 2A. Joule heating of up to 9°C is observed at the top surface of Gr-WSe₂-Gr junction. The hot spots indicate the inhomogeneity or defects at the interface. It is observed that the heat is mostly generated in the active layers and leaks through the graphene ribbons and gold contacts.

Fig. 5B shows the cooling curve obtained by using thermoreflectance imaging technique under low bias voltages up to ~0.06V. Using Eq. 1, we can estimate an equivalent ZT to be 1.5×10^{-3} for the Au-Gr-3WSe₂-Gr-Au structure. The boundary conditions used to obtain Eq. 1 is not satisfied in our experiment. First, the device is fabricated on a SiO₂ layer, which cannot dissipate the heat effectively and cannot serve as a perfect heat sink. Second, the cold side is not thermally isolated and there is a small heat leak due to convection, since the measurement is not performed in vacuum. Therefore, our measured ZT is considered to be underestimated for this device structure. While still too small for practical application, our measured ZT already shows three orders of magnitude enhancement compared with the previously reported ZT values for similar nanometer thick 2D layered heterostructures (17).

Discussion

To summarize, we have used first principles calculations combined with Green's function formalism to estimate the thermionic performance of Au-Gr-1 to 5 layers of WSe₂-Gr-Au

224 structures. We further fabricated the device and measured its performance to validate the theory.
225 The calculated transmission function indicated a clear suppression of tunneling current for
226 structures with more than 3 layers of WSe₂. Therefore, 3 layers is enough to build a thermionic
227 device. The calculated barrier height is 0.1 eV indicating that this device operates best at
228 temperatures above 600°K. The electronic conductance and the Seebeck coefficient, both increase
229 with temperature as shown in Fig. 4B. The room temperature calculated Seebeck coefficient is in
230 close agreement with the experimentally measured value of 72 $\mu\text{V/K}$ signifying the accuracy of the
231 calculations.

232
233 In the cross-plane direction, the thermal conductivity of WSe₂ layered structure has been reported
234 to be as low as $0.05 \text{ W m}^{-1} \text{ K}^{-1}$, which is among the lowest possible thermal conductivity values in
235 a solid (23). This ultra-low thermal conductivity, along with the large thermal boundary resistance
236 values reported for interfaces of 2D layered heterostructures, points to small values for the thermal
237 conductance of the studied structure.

238
239 The calculated lattice thermal conductance of $14 \text{ MWm}^{-2}\text{K}^{-1}$ for Au-Gr-3WSe₂-G-Au is close to
240 the measured value of $17 \text{ MWm}^{-2}\text{K}^{-1}$ for Gr-3WSe₂-Gr. The thermal conductance at Au-Gr
241 contacts is low and is about $20 \text{ MWm}^{-2}\text{K}^{-1}$. It is shown that the limited phonon density of states
242 in Au, is the determining factor in thermal transport at Au-Gr interfaces (24, 25). If we add the
243 thermal resistance of the Au-Gr contacts in series to the Gr-3WSe₂-Gr, we obtain a value of 6.3
244 $\text{MWm}^{-2}\text{K}^{-1}$. The experimentally measured conductance value is smaller than the theoretically
245 calculated ones due to the inevitable presence of defects. Values for similar structures have been
246 reported in the literature. Massicotte *et al.* reported a conductance of $0.5 \text{ MW m}^{-2} \text{ K}^{-1}$ for Au-Gr-
247 4WSe₂-Gr-Au (16). However, we note that the conductance reported reflects that of electron-
248 phonon coupling at Gr-hBN interfaces, a parallel process to the phonon mediated conductance

249 across these interfaces. Thus, we cannot make direct comparisons between values determined in
250 our work and those found in the literature. The contribution of electron-phonon coupling to the
251 conductance of 3- and 4-layer WSe₂ are reported to be similar due to the ballistic nature of transport
252 in these layers (16), however the total thermal conductance across metal-WSe₂-substrate interfaces
253 has been shown to decrease following an increase in the number of WSe₂ layers (26). The trend in
254 the latter is consistent with the ultralow thermal conductivity of WSe₂ (23), as the resistances
255 compound following an increase in the number of layers.

256
257 The I-V curve of the fabricated structure indicates a near-Ohmic contact. The overall electrical
258 conductance value calculated for the Au-Gr-3WSe₂-Gr-Au is small. For the fabricated structure
259 with the area of roughly $3\ \mu\text{m} \times 3\ \mu\text{m}$, the resistance is about $40\ \Omega$. Our contact resistance
260 measurements indicate Au-Ti-Gr contact varies from device to device and has a range from 0.5 to
261 $2\ \text{k}\Omega$. In other words, contact resistance is the dominant resistance in the experiment. If we use the
262 measured Seebeck coefficient, the calculated resistance and the measured thermal conductance, we
263 obtain a ZT of 7×10^{-4} for the current structure which is twice smaller than the directly measured
264 ZT value using thermoreflectance measurements. There are many sources of error when calculating
265 ZT from the three transport properties. First, while TDTR measurements are reliable for this
266 measurements, we used resistive model to add the thermal resistance of Au-Gr and Gr-3WSe₂-Gr
267 which only gives a rough idea about the overall thermal resistance of the device. Second, we were
268 not able to extract the electrical conductance of the device due to the large contact resistance and
269 hence we used the theoretical value for it. Finally, there are sample variations due to the presence
270 of defects and we note that the TDTR measurement was performed on a different sample.

271
272 The directly measured ZT value using thermoreflectance method, 1.5×10^{-3} , is small but it is
273 significantly larger compared with other similar structures. We have recently measured ZT of

monolayer and bilayer WSe₂ layers sandwiched between gold and graphite and only observed ZT values on the order of 10⁻⁵ due to the dominance of the tunneling current. Similarly, ZT of Gr-hBN-Gr is reported to be on the order of 10⁻⁶. Our measured ZT value is also consistent with the small calculated ZT values for this structure at room temperatures. As discussed before, the studied structure is suitable for elevated temperatures. To improve the ZT values at room temperatures, structures with lower electron energy barriers are needed. Barrier height of the current structure is 0.1eV. If we replace the gold contacts with another metal that can form a lower energy barrier (~0.05eV), we can extend the high performance of the device to room temperatures. We studied several possible metals. The most optimistic one for this structure is platinum. Transport properties of Pt-Gr-3WSe₂-Gr-Pt is reported in Fig. 4. The main advantage of Pt is to lower the energy barrier and therefore improve the electrical conductance. As shown in Fig. 4B two orders of magnitude enhancement in the electrical conductance is expected when replacing Au with Pt without deteriorating other transport properties.

Materials and Methods

Device Fabrication

A bottom graphene layer, 3 layers of WSe₂ and a top graphene layer were mechanically exfoliated and transferred on the substrate in sequence using a polydimethylsiloxane (PDMS)-assisted transfer method. The thickness of WSe₂ was identified by using optical contrasts on an optical microscope image of the WSe₂ on the PDMS where thicknesses of reference samples (from 1 to 5 layers) were measured by atomic force microscopy (AFM) and their optical contrasts in the green channel of a charge coupled device camera were served as reference values. Metal electrodes (Ti/Au-3nm/100nm) were deposited by using a general photolithography process and an electron-beam evaporation. The fabricated device was annealed at 200°C on a vacuum chamber overnight to achieve the Ohmic contact between metal and graphene.

299 **Transport Characterization**

300 The I-V curve of the device is measured using two probe method. The thermorefectance
301 measurement is based on the relative change in the reflectivity (due to change of refractive index)
302 of a device surface as a function of change in temperature, which can be represented by the
303 following first order relationship (27):

304

305
$$\frac{\Delta R}{R_o} = \left(\frac{1}{R_o} \frac{\delta R}{\delta T} \right) \Delta T = C_{th} \Delta T$$

306

307 where ΔR is the change in reflectivity, R is the reflected light, C_{th} is the thermorefectance
308 calibration coefficient and ΔT is the change in temperature. The calibration coefficient is typically
309 of the order of 10^{-2} to 10^{-5} and dependent on the sample material, the wavelength of the illuminating
310 light, the angle of incidence (and thus, by extension, the surface roughness) and the composition of
311 the sample in the case of multi-layer structures. Therefore, calibration for each material is required
312 to determine the exact value of calibration coefficient. The calibration method consists of heating
313 the sample using an external thermoelectric (TE) heating stage and a micro-thermocouple to record
314 the induced temperature change. The sample is heated at two distinct temperatures where the
315 reflectance distribution of the surface is measured. By measuring the change in reflectance, the
316 thermorefectance coefficient can be calculated at each location across the sample surface. The
317 measured calibration coefficient using 530nm LED on the overlap region of our sample is $2.0 (\pm$
318 $0.3) \times 10^{-4}$.

319

320 Thermorefectance measurement is carried out on the sample using the Microsanj NT220B system.
321 The thermorefectance measurement system consists of a pulse generator, a signal generator, and a
322 control unit. A 530nm green LED was used as an illuminator and was focused onto the sample's
323 top surface through a beam splitter and a high magnification objective. The reflected light that

324 contained the information on the samples surface temperature change was collected by a charge-
325 coupled device (CCD) detector. A 100 μ s voltage pulse was applied to the metallic contacts and the
326 temperature response of the sample was measured at 90 μ s. Steady state conditions was achieved
327 after 50 to 70 μ s.

328

329 We use time-domain thermoreflectance (TDTR) to characterize the conductance of the Gr-3WSe₂-
330 Gr structure. Our two-tint implementation of the technique is discussed elsewhere in the literature
331 (28), along with the associated analysis of the technique (29-31). We first coat a nominal 80 nm Al
332 transducer onto our Gr-3WSe₂-Gr structure, which has been mechanically exfoliated previously on
333 to silicon with a thermal oxide of 300 nm. The thickness of the Al was confirmed via picosecond
334 acoustics (32, 33), while it's thermal conductivity was determined from reference specimens placed
335 near to the Gr-3WSe₂-Gr sample during deposition. The effective $1/e^2$ pump/probe radii is ~ 1.5
336 μ m. The measured conductance at the Al-Gr-SiO₂ interface is found to be 20 MW m⁻² K⁻¹, while
337 that of the Al-Gr-3WSe₂-Gr-SiO₂ interfaces is 9 MW m⁻² K⁻¹. Because these two measurements
338 reflect the series resistances of the structures, we can use these values to determine the thermal
339 conductance of the Gr-3WSe₂-Gr structure alone. Doing so allows us to extract a conductance of
340 17 MW m⁻² K⁻¹ for the structure.

341 **Computational Methods**

342 To study the structural and electronic properties of the Au-Gr-WSe₂-Gr-Au van der Waals
343 heterostructure, we used the state-of-the-art density functional theory based first principles
344 calculations, as implemented in the Siesta package (34). We used the exchange-correlation
345 functional of Perdew-Burke-Ernzerhof (35) revised for solids (36) and standard basis set, namely,
346 double zeta plus polarization (DZP). Real space mesh cutoff energy was set to 300 Ry. A single k
347 point in the cross-plane direction whereas a 5 \times 5 \times 1 k mesh in the basal plane was used for the

Brillouin zone sampling. The in-plane lattice constants were fixed to the relaxed gold $\langle 111 \rangle$ plane while the graphene and WSe₂ lattices were adapted accordingly ($2\sqrt{3}a_{\text{Au}\langle 111 \rangle} = 4a_{\text{Gr}} = \sqrt{7}a_{\text{WSe}_2}$, a is the lattice constant). The cross-plane direction was relaxed without any constraint. The forces of all the atoms were relaxed within 0.01 eV/Å. The ballistic transport properties were calculated using the real space Green's function method as in the TranSiesta implementation (37). Phonon thermal conductance was calculated using Green's function method simplified for 1D model (9).

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General: This publication is dedicated to the memory of Prof. Mildred Dresselhaus (1930-2017) who served the scientific community not only with her broad knowledge of physics and science policy, but also by empowering young scientists from diverse backgrounds. She was a role model and a source of inspiration for the scientific community including the authors of this paper.

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Supplementary Materials

Section S1. Series Resistor Model.

Section S2. Analysis of contact resistance.

Fig. S1. Time-domain thermoreflectance measurement.

Fig. S2. Figure of merit (ZT) of Au-G-WSe₂-G-Au structure and Pt-G-WSe₂-G-Pt structure.

Fig. S3. Repeatable cooling curve measurement.

Fig. S4. Contact resistance measurement.

Table S1. Two probe resistance data for sample 1 and sample 2.

Table S2. Four probe resistance data for sample 1 and sample 2.

Table S3. Contact resistances.

Figures and Tables

Fig. 1. Au-Gr-3WSe₂-Gr-Au device. (A) Illustration of the cross-section of the Au-Gr-3WSe₂-Gr-Au structure. The 3 layers of WSe₂ flake is sandwiched by top and bottom graphene layers on a Si/SiO₂ substrate and contact metals (Ti/Au) are deposited on top and bottom graphene layers. (B) Optical microscope image of an Au-Gr-3WSe₂-Gr-Au device. The 3 layers WSe₂, top graphene and bottom graphene are highlighted by red, white and black dashed lines, respectively. The scale bar corresponds to 20 μm . (C) I-V curve of the fabricated Au-Gr-3WSe₂-Gr-Au device.

Fig. 1. Seebeck measurement. (A) Schematic of the Seebeck measurement setup. (B) The Seebeck voltage measured vs. applied temperature difference. The measured Seebeck coefficient is 72 ± 12 $\mu\text{V/K}$.

Fig. 3. Electronic Structure of Au/Pt-Gr-WSe₂-Gr-Au/Pt. (A) Ball-stick model for the configuration of Au/Pt-Gr-WSe₂-Gr-Au/Pt. The yellow, green, grey, and brown balls denote Au/Pt, Se, W, and C atoms, respectively. (B) Contour plot of the local density of states (LDOS) of Au-Gr-WSe₂-Gr-Au structure. The horizontal axis shows the positions of different layers. (C) Contour plot of the local density of states (LDOS) of Pt-Gr-WSe₂-Gr-Pt structure. The horizontal axis shows the positions of different layers.

Fig. 4. Transport Properties of Au/Pt-Gr-WSe₂-Gr-Au/Pt. (A) Electron transmission function in the cross-plane direction of gold structure (solid blue line) and platinum structure (red dotted line). (B) Calculated Seebeck coefficient (S, red line) and electrical conductance (G, blue line) vs temperature of both gold and platinum structure. The red circle is the experimentally measured Seebeck coefficient at room temperature (C) Phonon transmission function in the cross-plane direction of gold structure (solid blue line) and platinum structure (red dotted line). (D) Calculated electronic thermal conductance (G_e, red line) and lattice thermal conductance (G_{ph}, blue line) vs temperature of both gold and platinum structure.

Fig. 2. Thermal imaging of the Joule heating inside the structure and cooling curve. (A) Joule heating: 2D temperature map of Au-Gr-WSe₂-Gr-Au device under a relatively high voltage 2V obtained using thermoreflectance method. Joule heating dominates in the Gr-WSe₂-Gr junction, and leaks through the graphene ribbon and gold contacts. (B) Cooling curve: Temperature difference between the substrate and top of the active device in Kelvin vs. applied voltage at small applied voltages.